



西北工业大学

NORTHWESTERN POLYTECHNICAL UNIVERSITY



# 程序册

P R O G R A M

## 第七届西安国际图论与组合数学研讨会

The 7th Xi'an International Workshop on Graph Theory and Combinatorics

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# The 7th Xi'an International Workshop on Graph Theory and Combinatorics

Northwestern Polytechnical University

Xi'an, Shaanxi, P.R. China

June 23-June 28, 2023

## Location

Xi'an Guangcheng Hotel, Xi'an, P.R. China

ZOOM Meeting ID: 302 412 8953, Passcode: xian

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# The 7th Xi'an International Workshop on Graph Theory and Combinatorics

## Program

Location: Xi'an Guangcheng Hotel; Online ZOOM ID: 302 412 8953; Passcode: xian			
June 24, Saturday			
08:30-09:00	Opening Ceremony      Chair: Shenggui Zhang		
Beijing Time	Chair	Speaker	Title
09:00-09:40	Xueliang Li	Gyula O. H. Katona	Combinatorial search problems
09:40-10:20		Dragan Stevanovic	Constructing examples and counterexamples in graph theory with reinforcement learning
10:20-10:40	Tea Break		
10:40-11:20	Wei Wang	Sanming Zhou	An overview of perfect codes in Cayley graphs (online)
11:20-12:00		Binzhou Xia	Card shuffle groups (online)
12:00-14:00	Lunch		
14:00-14:40	Shenggui Zhang	Miklós Simonovits	Stability methods in extremal combinatorics, and their role in proofs (online)
14:40-15:20		Gregory Gutin	Maximum digraph partitions (online)
15:20-15:40	Tea Break		
15:40-16:20	Ligong Wang	Shinya Fujita	Orientations for properly ordered coloring of vertex weighted graphs (online)
16:20-17:00		Yaping Mao	Gallai-Rado numbers and their multiplicities
17:00-17:40		Jingtao Zang	A rank of partitions with overline designated summands
18:00-20:00	Dinner		

Location: Xi'an Guangcheng Hotel; Online ZOOM ID: 302 412 8953; Passcode: xian			
June 25, Sunday			
08:30-09:10	Yandong Bai	Jie Han	Spanning trees in sparse expanders
09:10-09:50		Suil Oh	Eigenvalues and factors in graphs
09:50-10:10	Tea Break		
10:10-10:50	Xin Zhang	Bofeng Huo	Supereulerian regular matroids
10:50-11:30		Xia Zhang	The Turán number of bipartite degenerate graphs
11:30-12:00		Ruijuan Li	The oriented diameter of a bridgeless graph with the given path $P_k$
12:00-14:00	Lunch		
14:00-14:30	Fenjin Liu	Zhouningxin Wang	Modulo $k$ -orientation and homomorphism to cycles
14:30-15:00		Jiangdong Ai	On Seymour's and Sullivan's Second-Neighbourhood Conjectures
15:00-15:30		Jian Wang	Intersecting families with covering number three
15:30-16:00		Bo Deng	Graph entropy based on strong coloring of uniform hypergraphs
16:00-16:20	Tea Break		
16:20-16:40	Ruonan Li	Jimeng Xiao	Turán numbers and anti-Ramsey numbers for short cycles
16:40-17:00		Shasha Zheng	Graphical regular representations of finite groups
17:00-17:20		Fangfang Wu	Properly colored and rainbow $C_4$ 's in edge-colored graphs (online)
17:20-17:40		Jing Wang	Fractional revival on Cayley graphs and semi-Cayley graphs
17:40-18:00	Closing Ceremony      Chair: Shenggui Zhang		

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# Abstract

## 1 On Seymour's and Sullivan's second-neighbourhood conjectures

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In this talk, we will introduce a sufficient condition in terms of the number of transitive triangles for an oriented graph to satisfy Sullivan's conjecture. We also show that the two conjectures hold for some families of oriented split graphs, in particular, when the tournament is regular or almost regular.

## 2 Graph entropy based on strong coloring of uniform hypergraphs

Bo Deng  
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The classical graph entropy based on the vertex coloring proposed by Mowshowitz depends on a graph. In fact, a hypergraph, as a generalization of a graph, can express complex and high-order relations such that it is often used to model complex systems. Being different from the classical graph entropy, we extend this concept to a hypergraph. Then, we define the graph entropy based on the vertex strong coloring of a hypergraph. Moreover, some tightly upper and lower bounds of such graph entropies as well as the corresponding extremal hypergraphs are obtained.

## 3 Orientations for properly ordered coloring of vertex weighted graphs

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Let  $(G, w)$  be a vertex weighted graph, where  $w$  is a weight function on  $V(G)$  such that  $w : V(G) \rightarrow \{1, 2, \dots\}$ . A vertex coloring  $c : V(G) \rightarrow \{0, 1, 2, \dots\}$  is *properly ordered coloring* (POC) of  $(G, w)$ , if for every edge  $e = uv$  in  $E(G)$ ,  $c(u) > c(v)$  if  $w(u) > w(v)$  and  $c(u) \neq c(v)$  if  $w(u) = w(v)$ . This notion was introduced in [S. Fujita, S. Kitaev, S. Sato, L-D. Tong: On properly ordered coloring of vertices in a vertex-weighted graph. *Order* 38: 515-525 (2021)].

In this talk, we consider giving an orientation on  $E(G)$  such that the in-degrees of vertices of the resulting digraph  $D$  achieve a POC on  $(G, w)$  for the case where  $G$  is a tree  $T$  and  $w : V \rightarrow \{1, 2\}$ . Some recent results in this topic will be reviewed.

## 4 Maximum digraph partitions

Gregory Gutin

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This talk is based on two recent papers: (1) J. Ai, S. Gerke, G. Gutin, A. Yeo and Y. Zhou, Bounds on Maximum Weight Directed Cut, arXiv:2304.10202, (2) A. Deligkas, E. Eiben, G. Gutin, P.R. Neary and A. Yeo, Complexity of Efficient Outcomes in Binary-Action Polymatrix Games with Implications for Coordination Problems, Proc. IJCAI 2023, also arXiv:2305.07124.

In the first part of the talk, we'll discuss lower and upper bounds for Max Weighted Directed Cut. We'll compare our results with those obtained for the maximum size of a directed cut in unweighted digraphs. In particular, we see that a lower bound obtained by Alon, Bollobas, Gyafas, Lehel and Scott (J Graph Theory 55(1) (2007)) for unweighted acyclic digraphs can be extended to weighted digraphs with the maximum length of a cycle being bounded by a constant and the weight of every arc being at least one.

In the second part of the talk, we'll discuss complexity dichotomies (in P or NP-hard) proved for the new problem termed Maximum Weighted Digraph Partition (MWDP), which generalizes Maximum Weight Directed Cut and a number of other optimization problems on directed and undirected graphs. One of the dichotomies implies a complexity dichotomy for max welfare in general binary-action polymatrix games.

## 5 Supereulerian regular matroids

Bofeng Huo

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The concept of matroid partly originates from matrix. A regular matroid is isomorphic to the vector matroid of a full unimodular matrix. A cycle of a matroid is a disjoint union of circuits. A matroid is supereulerian if it contains a spanning cycle. It is well known that every simple graph  $G$  with  $n = |V(G)|$  and minimum degree  $\delta(G) \geq \frac{n}{2}$  is Hamiltonian, thus supereulerian. To answer an open problem of Bauer in 1985, Catlin proved in [J. Graph Theory 12 (1988) 29-44] that for sufficiently large  $n$ , every 2-edge-connected simple graph  $G$  with  $n = |V(G)|$  and minimum degree  $\delta(G) \geq \frac{n}{5}$  is supereulerian. Lai proved in [J. Graph Theory 12 (1988) 11-15] that for sufficiently large  $n$ , every 2-edge-connected simple graph  $G$  with  $n = |V(G)|$  and minimum degree  $\delta(G) \geq \frac{n}{10}$  is supereulerian or its reduction is  $K_{2,3}$ . To find corresponding results like these conclusions in matroid is a research interest. In [European J. Combinatorics, 33 (2012), 1765-1776], it is shown that for any connected simple regular matroid  $M$ , if every cocircuit  $D$  of  $M$  satisfies  $|D| \geq \max\{\frac{r(M)-5}{5}, 6\}$ , then  $M$  is supereulerian. We find that (i) For any real number  $c$  with  $0 < c < 1$  there exists an integer  $f(c)$  such that if every cocircuit  $D$  of a connected simple cographic matroid  $M$  satisfies  $|D| \geq \max\{c(r(M)+1), f(c)\}$ , then  $M$  is supereulerian. (ii) Let  $M$  be a connected simple regular matroid. If every cocircuit  $D$  of  $M$  satisfies  $|D| \geq \max\{\frac{r(M)+1}{10}, 8\}$ , then  $M$  is supereulerian. (ii) Let  $M$  be a connected simple regular matroid. If every cocircuit  $D$  of  $M$  satisfies  $|D| \geq \max\{\frac{r(M)+1}{15}, 9\}$  and  $M$ 's girth  $g(M) \geq 4$ , then  $M$  is supereulerian.

## 6 Spanning trees in sparse expanders

Jie Han

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We consider the spanning tree embedding problem in dense graphs without bipartite holes and sparse graphs. In 2005, Alon, Krivelevich and Sudakov asked for determining the best possible spectral gap forcing an  $(n, d, \lambda)$ -graph to be  $T(n, \Delta)$ -universal. In this talk, we introduce our recent work on this conjecture.

## 7 Combinatorial search problems

Gyula O. H. Katona

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Suppose that in a certain  $n$ -element population, denoted by  $[n]$ , there is exactly one infected person. Obviously, one has to take a blood or saliva sample from every individual, therefore the expenses can be reduced only reducing the number of chemical tests. It was observed by Dorfman and Sterrett that it is not necessary to test every sample one by one, but one can form subsets of the samples, testing them together. This method is called “group testing” or “combinatorial search”.

Mathematically the model is the following. Subsets  $A \subset [n]$  can be tested if the unknown element  $x$  is in  $A$  or not. The unknown  $x$  is to be found on the basis of the answers. There are two main versions. When the next test set is chosen depending the previous answers, the search is called *adaptive*, while in the case when the family  $A_1, A_2, \dots, A_m$  of test sets is given in advance then the search is called *non-adaptive*. It is easy to see that, if any subset  $A \subset [n]$  can be used as a test set then the search can be carried out in  $\lceil \log n \rceil$  steps (even in the non-adaptive case). However in practical situation the test sets can be chosen only from a family  $\mathcal{A}$  of subsets of  $[n]$ . Rényi suggested to find the minimum number of tests if  $\mathcal{A}$  consist of all sets of size at most  $k$  when  $k$  is a relatively small integer. (This is a natural assumption in the case of finding the infected person.) Both the adaptive and the non-adaptive cases were solved by the author in 1966. The non-adaptive case can be formulated in the following way: find the minimum number of subsets of  $[n]$  of at most  $k$  elements such that for any two distinct elements  $x, y \in [n]$ , there is a set separating them.

There are any variants of this model following the several practical applications.

One of the important variants is when the answer to the question “is  $x \in A$ ?” can be incorrect. Because of a human error or some dirt spoils the chemical test. This is called *search in presence of a liar* or the *Rényi-Ulam game*. Here, again, one is looking for the unknown element  $x \in [n]$  by asking questions of form “is  $x \in A$ ?”. However it is supposed that at most  $\ell$  answers can be incorrect. Yet, the unknown element should be found without an error. The mathematical problem here is to find the minimum number of tests needed (in both, adaptive and non-adaptive cases). A good survey was written by Deppe in 2007.

In the cases above, in the traditional model of “search in presence of liar”, the lies come independently. In some applications, however there might be connections among the test, the unknown  $x$  and the lie. For instance when  $x$  is the perpetrator in a criminal investigation then the answer to a question to the eyewitness can be incorrect depending on  $x$ . Say, if  $x$  is a friend of the witness. This situation can be described in the following way. Here instead of asking “is  $x \in A$  or in its complement?” there is a certain subset  $L$  and the answer can be incorrect if  $x$  is in  $L$ . Otherwise it is surely correct. Mathematically in



this case the following model is considered. There is exactly one unknown element in  $[n]$ . A question is a partition of  $[n]$  into three classes:  $(A, L, B)$ . If  $x \in A$  then the answer is “yes” (or 1), if  $x \in B$  then the answer is “no” (or 0), finally if  $x \in L$  then the answer can be either “yes” or “no”. In other words, if the answer “yes” is obtained then we know that  $x \in A \cup L$  while in the case of “no” answer the conclusion is  $x \in B \cup L$ . The mathematical problem is to minimize the minimum number of questions under certain assumptions on the sizes of  $A, B$  and  $L$ . This problem has been solved under the condition  $|L| \geq r$  by the author and Krisztián Tichler in previous papers for both the adaptive and non-adaptive cases.

In the present work we suggest to solve the problems under the conditions  $|A| \leq a, |B| \leq b$ . The adaptive case is completely solved. Let us make clear that the problem in the non-adaptive case is a problem of Extremal Set Theory. The minimum number of partitions  $(A, L, B)$  should be determined under the conditions  $|A| \leq a, |B| \leq b$  and that for any two distinct elements  $x, y \in [n]$  there is a partition strongly separating them that is one of the is in  $A$ , the other one is in  $B$ . We present asymptotic solutions. Among others the concept of *graph entropy* is used what was introduced by Körner.

## 8 The oriented diameter of a bridgeless graph with the given path $P_k$

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Let  $G = (V, E)$  be a bridgeless undirected graph. The oriented diameter of  $G$ , denoted by  $\overrightarrow{\text{diam}}(G)$ , is the minimum diameter of any strongly connected orientation of  $G$ . Dankelmann, Guo and Surmacs [J. Graph Theory, 88 (2018), 5-17] showed that every bridgeless graph  $G$  of order  $n$  has an oriented diameter at most  $n - \Delta + 3$ , where  $\Delta$  is the maximum degree of  $G$ . Let  $N_G(H) = \bigcup_{v \in V(H)} N_G(v) \setminus V(H)$  for a subgraph  $H$  of  $G$ . For an edge  $e$ , they proved that  $G$  has an orientation of diameter at most  $n - |N_G(e)| + 5$ . In this report, we discuss how the above-mentioned upper bound to be generalized to  $\overrightarrow{\text{diam}}(G) \leq n - |N_G(P_k)| + 2 \lfloor \frac{k}{2} \rfloor + 3$  by substituting a vertex or an edge  $e$  by a given path  $P_k$  in  $G$  and provide the examples to show the sharpness of the upper bound. We also introduce the current research status and progress related to the topics.

## 9 Gallai-Rado numbers and their multiplicities

Yaping Mao  
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Ramsey theory on the integers covers a variety of topics from the field of Ramsey theory, limiting its focus to the set of integers. In this talk, we will introduce some short history of Rado numbers, the concept of Gallai-Rado numbers and Gallai-Ramsey multiplicity. It includes some recent work by us on this topic.

## 10 Eigenvalues and factors in graphs

Suil Oh

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In this talk, we investigate spectral conditions for an ( $r$ -regular) graph to guarantee the existence of a certain factor.

## 11 Stability methods in extremal combinatorics, and their role in proofs

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The notion of stability is very important in physics and in the theory of Differential Equations. Somewhat surprisingly, it became also an important notion in Discrete Mathematics

This lecture is part of a longer one which is based on a joint manuscript of Zoltán Füredi and myself.

In this lecture we shall describe one of the most powerful methods of Extremal Combinatorics, the Stability Method. The Erdős-Simonovits Stability theorem asserts that in case of ordinary graphs and Turán type extremal problems the extremal graphs and more generally, the almost extremal graphs have almost the same structure as in case of Turán's theorem. This theorem can be used in various settings, among others to prove sharp theorems, and also to prove results for extremal subgraphs of Random Graphs, like in the proof of the Babai-Simonovits-Spencer theorem. This area is related to several distinct branches of Discrete Mathematics. We shall discuss the stability approach in several distinct situation.

Among others we shall discuss the connection to the Regularity Lemma, and to the question how a result of Füredi helps to obtain a new proof of the Erdős-Simonovits stability theorem.

## 12 Constructing examples and counterexamples in graph theory with reinforcement learning

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Despite the tendency of mathematicians to present only finished, elegant results, experiment has always been an important part of mathematical discovery, serving either to lead a way towards new constructions or to refute ill-posed conjectures. We will discuss here the recently proposed new approach of Adam Wagner [arXiv:2104.14516 (2021)] of using an old reinforcement learning method to construct (counter)examples in graph theory. Besides explaining its inner workings, we will showcase here our more digestible re-implementation that is further sped up by combining Python's machine learning capabilities with the speed of computing (spectral) graph invariants in Java, and present counterexamples that have been found for a few conjectures along the way...

## 13 Intersecting families with covering number three

Jian Wang

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We consider  $k$ -graphs on  $n$  vertices, that is,  $\mathcal{F} \subset \binom{[n]}{k}$ . A  $k$ -graph  $\mathcal{F}$  is called intersecting if  $F \cap F' \neq \emptyset$  for all  $F, F' \in \mathcal{F}$ . In the present paper we prove that for  $k \geq 7$ ,  $n \geq 2k$ , any intersecting  $k$ -graph  $\mathcal{F}$  with covering number at least three, satisfies  $|\mathcal{F}| \leq \binom{n-1}{k-1} - \binom{n-k}{k-1} - \binom{n-k-1}{k-1} + \binom{n-2k}{k-1} + \binom{n-k-2}{k-3} + 3$ , the best possible upper bound which was proved by Frankl subject to exponential constraints  $n > n_0(k)$ . Joint work with Peter Frankl.

## 14 Fractional revival on Cayley graphs and semi-Cayley graphs

Jing Wang

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Quantum state transfer in quantum networks is a very important research content for quantum communication protocols. Let  $G$  be a graph and  $A_G$  the adjacency matrix of  $G$ . The *transition matrix* of  $G$  relative to  $A_G$  is defined by  $H_{A_G}(t) = \exp(itA_G)$ . If  $u$  and  $v$  are distinct vertices in  $G$ , we say that  $G$  admits *fractional revival* from  $u$  to  $v$  if there is a time  $\tau$  such that  $|H_{A_G}(\tau)_{u,u}|^2 + |H_{A_G}(\tau)_{u,v}|^2 = 1$ . In this talk, we will show what we have obtained on existence of fractional revival on Cayley graphs and semi-Cayley graphs over finite abelian groups. This is a joint work with Ligong Wang and Xiaogang Liu.

## 15 Modulo $k$ -orientation and homomorphism to cycles

Zhouningxin Wang

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It is well-known that a graph admits a circular  $(2k+1)/k$ -flow if and only if it admits a modulo  $(2k+1)$ -orientation. When restricted to planar graphs, a plane graph admits a modulo  $(2k+1)$ -orientation if and only if its dual plane graph  $G^*$  admits a homomorphism to an odd cycle of length  $2k+1$ . In this talk, generalizing these notions to signed graphs, we shall explore the relation between modulo  $k$ -orientations on signed graphs and homomorphisms to signed cycles. In particular, we will show every  $(6k-2)$ -edge-connected Eulerian signed graph admits a modulo  $2k$ -orientation, and every signed bipartite planar graph of negative girth at least  $6k-2$  admits a homomorphism to a negative even cycle of length  $2k$ . This is joint work with Jiaao Li, Reza Naserasr, and Xuding Zhu.

## 16 Properly colored and rainbow $C_4$ 's in edge-colored graphs

Fangfang Wu

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We present new sharp sufficient conditions for the existence of properly colored and rainbow  $C_4$ 's in edge-colored graphs. Our first results deal with sharp color neighborhood conditions for the existence of properly colored  $C_4$ 's in edge-colored complete graphs and complete bipartite graphs, respectively. Next, we characterize the extremal graphs for an anti-Ramsey number result due to Alon on the existence of rainbow  $C_4$ 's in edge-colored complete graphs. We also generalize Alon's result from complete to general edge-colored graphs. Finally, we derive a structural property regarding the extremal graphs for a bipartite counterpart of Alon's result due to Axenovich, Jiang and Kündgen on the existence of rainbow  $C_4$ 's in edge-colored complete bipartite graphs. We also generalize their result from complete to general bipartite edge-colored graphs.

## 17 Card shuffle groups

Binzhou Xia

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Shuffling a deck of cards is often encountered in card tricks. There are a number of questions that may be of concern, such as how a shuffle changes the order of the deck, and how many different orderings can be obtained by shuffling the deck repeatedly. The latter question is to determine the permutation group, called the shuffle group, generated by all the considered shuffles. More precisely, for positive integers  $k$  and  $n$ , the shuffle group  $G_{k,kn}$  is generated by the  $k!$  permutations of a deck of  $kn$  cards performed by cutting the deck into  $k$  piles with  $n$  cards in each pile, and then perfectly interleaving these cards following certain order of the  $k$  piles. The shuffle group  $G_{2,2n}$  was completely determined by Diaconis, Graham and Kantor in 1983, and a conjectural classification has been made in the literature for the general  $G_{k,kn}$ . In this talk, we confirm this conjecture in the case when  $k \geq 4$  or  $k$  does not divide  $n$ . For the remaining case, we reduce the proof of the conjecture to that of the 2-transitivity of the shuffle group. This is joint work with Zhishuo Zhang and Wenying Zhu.

## 18 Turán numbers and anti-Ramsey numbers for short cycles

Jimeng Xiao

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We call a 4-cycle in  $K_{n_1, n_2, n_3}$  multipartite, denoted by  $C_4^{\text{multi}}$ , if it contains at least one vertex in each part of  $K_{n_1, n_2, n_3}$ . The Turán number  $\text{ex}(K_{n_1, n_2, n_3}, C_4^{\text{multi}})$  (respectively,  $\text{ex}(K_{n_1, n_2, n_3}, \{C_3, C_4^{\text{multi}}\})$ ) is the maximum number of edges in a graph  $G \subseteq K_{n_1, n_2, n_3}$  such that  $G$  contains no  $C_4^{\text{multi}}$  (respectively,  $G$  contains neither  $C_3$  nor  $C_4^{\text{multi}}$ ). We call an edge-colored  $C_4^{\text{multi}}$  rainbow if all four edges of it have different colors. The anti-Ramsey number  $\text{ar}(K_{n_1, n_2, n_3}, C_4^{\text{multi}})$  is the maximum number of colors in an edge-colored  $K_{n_1, n_2, n_3}$  with no rainbow  $C_4^{\text{multi}}$ . In this paper, we determine that  $\text{ex}(K_{n_1, n_2, n_3}, C_4^{\text{multi}}) = n_1 n_2 + 2n_3$  and  $\text{ar}(K_{n_1, n_2, n_3}, C_4^{\text{multi}}) = \text{ex}(K_{n_1, n_2, n_3}, \{C_3, C_4^{\text{multi}}\}) + 1 = n_1 n_2 + n_3 + 1$ , where  $n_1 \geq n_2 \geq n_3 \geq 1$ .

## 19 A rank of partitions with overline designated summands

Wenston J.T. Zang

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Andrews, Lewis and Lovejoy introduced the partition function  $PD(n)$  as the number of partitions of  $n$  with designated summands. Lin studied a partition function  $PD_t(n)$  which counts the number of tagged parts over all the partitions of  $n$  with designated summand. He proved that  $PD_t(3n+2)$  is divisible by 3. In this talk, we will first introduce a combinatorial structure named partitions with overline designated summands, which counted by  $PD_t(n)$ . We then define a generalized rank on this structure, which provide a combinatorial interpretation of the congruence of  $PD_t(3n+2)$ . (This is joint work with Robert X.J. Hao and Erin Y.Y. Shen)

## 20 The Turán number of bipartite degenerate graphs

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In 1966, Erdős put forward a conjecture that the Turán number of every bipartite  $r$ -degenerate graph  $H$  is  $ex(n, H) = O(n^{2-\frac{1}{r}})$ . In this talk, we define a class of  $r$ -degenerate bipartite graph  $F(r, l, m)$  and show that  $ex(n, F(r, l, m)) = O(n^{2-\frac{1}{r}})$ . This result extends the ones of Grzesik, Janzer and Nagy in 2019 on the Turán number of  $r$ -degenerate blow-ups of trees [The Turán number of blow-ups of trees. J. Comb. Theory, Ser. B 156 (2019): 299-309.].

## 21 Graphical regular representations of finite groups

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In this talk we are concerned with the automorphisms of Cayley graphs. Here are some natural questions: What kind of automorphism group of a Cayley graph is ‘typical’; what kind of Cayley graph is ‘common’? Viewing that ‘symmetry is rare’, a rough guess for the first question would be the groups that are ‘as small as possible’ in some sense, and one may guess for the second question that the Cayley graphs having the ‘smallest’ full automorphism groups would be the most common ones. We estimate the number of graphical regular representations of a given group with large enough order and show that almost all finite Cayley graphs have full automorphism groups ‘as small as possible’. This confirms a conjecture of Babai-Godsil-Imrich-Lovasz. (This is joint work with Binzhou Xia.)

## 22 An overview of perfect codes in Cayley graphs

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For a graph  $\Gamma$  and a positive integer  $e$ , a perfect  $e$ -code in  $\Gamma$  is a subset  $C$  of  $V(\Gamma)$  such that the closed  $e$ -neighbourhoods of the vertices in  $C$  form a partition of  $V(\Gamma)$ . Given a finite group  $G$  and an inverse-closed subset  $S$  of  $G$  excluding the identity element, the Cayley graph  $\text{Cay}(G, S)$  is the graph with vertex set  $G$  such that  $x, y \in G$  are adjacent if and only if  $yx^{-1} \in S$ . Perfect codes in Cayley graphs can be considered as generalisations of perfect codes in classical coding theory, and perfect 1-codes in Cayley graphs are closely related to tilings of the underlying groups. I will give an overview of perfect codes in Cayley graphs with a focus on perfect 1-codes.

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